

Problemen

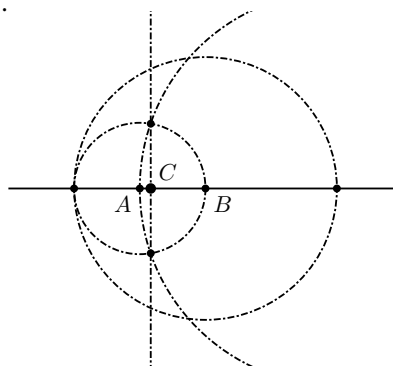
| Problem Section

Edition 2010-3 We received solutions from: Maurice Bos (Delft), Pieter de Groen (Brussel), Thijmen Krebs (Nootdorp), Tejaswi Navilarekallu (Amsterdam), José H. Nieto (Maracaibo), and Sep Thijssen (Nijmegen).

All three problems asked for a construction with ruler and compass in a limited number of steps. More precisely, given a collection of points, lines, and circles in the plane, a *move* consists of adding to the collection either a line through two of the points, or a circle centered at one of them and passing through another. At any time one is allowed to freely add any intersection point among the lines and circles, as well as any sufficiently general point, either in the plane, or on any of the lines or circles.

Problem 2010-3/A Given a line and distinct points A and B on it, construct in at most four moves the point C between A and B that satisfies $6|AC| = |AB|$.

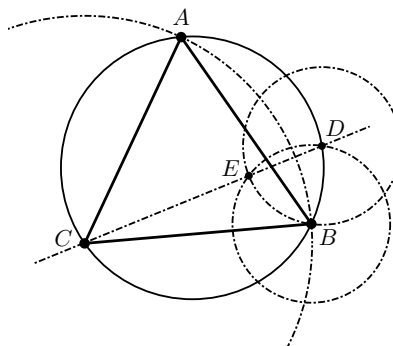
Solution This problem was solved by Pieter de Groen, Thijmen Krebs, Tejaswi Navilarekallu, José H. Nieto, and Sep Thijssen. All found the construction above. Pieter de Groen receives the book token (by random draw).



Problem 2010-3/B Given a circle, but not its center, construct in at most seven moves an equilateral triangle whose vertices lie on the circle.

Solution This problem was solved by Maurice Bos, Pieter de Groen, Thijmen Krebs, Tejaswi Navilarekallu, and José H. Nieto. All found the following construction. Thijmen Krebs receives the book token (by random draw).

Let B and D be two distinct points on the given circle. We start with two circles, one centered in B and going through D , the other centered in D and going through B . We then proceed as follows.



To see the correctness of this construction, note $\angle CDB = \angle EDB = \pi/3$, and as the angles CDB and CAB stand on the same chord, $\angle CAB$ equals $\pi/3$ as well.

Redactie:

Johan Bosman

Gabriele Dalla Torre

Ronald van Luijk

Lenny Taelman

Problemenrubriek NAW

Mathematisch Instituut

Universiteit Leiden

Postbus 9512

2300 RA Leiden

problems@nieuwarchief.nl

www.nieuwarchief.nl/problems

Oplossingen

| Solutions

Problem 2010-3/C Construct a square in at most eight moves.

Solution This problem was solved by Pieter de Groen, Thijmen Krebs, Tejaswi Navilarekallu, and José H. Nieto. All found the following construction. Tejaswi Navilarekallu receives the book token (by random draw).

