Problem Section

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Redactie:

Problem A (proposed by Hendrik Lenstra)

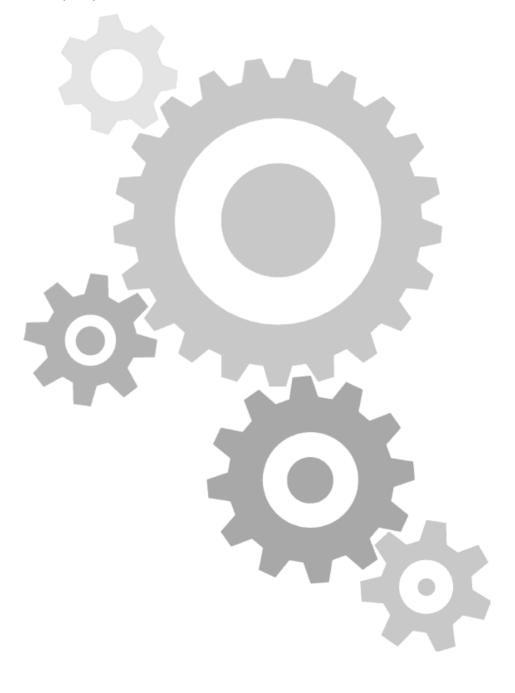
Let *m* and *n* be coprime positive integers. Let Γ be the graph that has the disjoint union $\mathbb{Z}/n\mathbb{Z} \sqcup \mathbb{Z}/m\mathbb{Z}$ as vertex set and that has for every $1 \le i \le m + n - 1$ an edge connecting $i \mod n$ and $i \mod m$. Show that Γ is a tree.

Problem B (proposed by Gabriele Dalla Torre)

Is it possible to partition a non-empty open interval in closed intervals of positive length? Let Δ be a triangle (including its interior) and let $P \in \Delta$ be an interior point. Is it possible to partition $\Delta - \{P\}$ in closed line segments of positive length?

Problem C (proposed by Tejaswi Navilarekallu)

A move on a pair (a, b) of integers consists of replacing it with either (a + b, b) or (a, a + b). Show that starting from any pair of coprime positive integers one can obtain a pair of squares in finitely many moves.



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